

MATH 1010 ~ Intermediate Algebra

Chapter 5: POLYNOMIALS AND
FACTORING**Section 5.5: Factoring Trinomials**

Objectives:

- * Recognize and factor perfect square trinomials.
- * Factor Trinomials of varying forms.
- * Factor polynomials using guidelines for factoring.

$$\begin{array}{l} x^2 - 6x + 9 = (\quad) \\ \times \\ x^2 + 3x - 4 = (\quad) \end{array}$$
$$6x^3 + 27x^2 - 15x = (\quad)(\quad)$$

Perfect Square Trinomials

$$\begin{array}{l} \textcircled{1} \quad u^2 + 2uv + v^2 = (u + v)^2 \\ \textcircled{2} \quad u^2 - 2uv + v^2 = (u - v)^2 \end{array}$$

$$\begin{aligned} (u+v)^2 &= (u+v)(u+v) \\ &= u^2 + uv + uv + v^2 \end{aligned}$$

① EXAMPLES:

a) $x^2 - 4x + 4 = x^2 - 2(2x) + 2^2$ ②
 $= (x-2)^2$ $x = u$
 $2 = v$

b) $9x^2 - 30xy + 25y^2 = (3x)^2 - 2(15xy) + (5y)^2$
 $\textcircled{2} \quad u = 3x \quad = (3x - 5y)(3x - 5y)$
 $v = 5y \quad = (3x - 5y)^2$

c) $16x^3 + 80x^2 + 100x$

$$\begin{array}{l} = 4x(4x^2 + 20x + 25) \\ \textcircled{1} \quad u = 2x \quad = 4x((2x)^2 + 2(10x) + 5^2) \\ v = 5 \quad | \quad = 4x(2x + 5)^2 \end{array}$$

- ② EXAMPLE:
Factor these.

Guess & Test

a) $x^2 - x - \underline{20}$?
 $= (\cancel{x-2})(\cancel{x+10})$ $8x \neq -x$
 $\cancel{(x-4)(x+5)}$ $-4x+5x = x \neq -x$
 $\boxed{(x+4)(x-5)}$

b) $x^2 - 17x - \underline{18}$
 $= (\cancel{x-18})(\cancel{x+1})$

c) $x^2 + 5x + \underline{4}$
 $= (\cancel{x+2})(\cancel{x+2})$
 $= \boxed{(x+4)(x+1)}$

(3) EXAMPLE:

Factor these.

a) $\underline{4x^2 + 5x - 6}$
 ~~$= (2x - 3)(2x + 2)$~~
 ~~$= (2x - 1)(2x + 6)$~~

~~$(4x+3)(x-2)$~~
 ~~$(4x-3)(x+2)$~~

b) $\underline{2x^2 - x - 3}$

$2 \cdot -3 = -6$
 $-1, 6$
 $-6, 1$
 $-2, 3$
 $\textcircled{2, -3}$

$-x = 2x - 3x$
 $(x+1)(2x-3)$

\times

$2x$	-3
$2x^2$	$-3x$
$2x$	-3

c) $6x^2 + 19x + 10$

$6 \cdot 10 = 60$
 $1, 60$
 $2, 30$
 $3, 20$
 $\textcircled{4, 15}$

$2x$ 5

$3x$	$6x^2$	$15x$
2	$4x$	10

$19x = 4x + 15x$

$(3x+2)(2x+5)$

- ④ EXAMPLE:
Factor these.

a) $-3x^2 + 16x + 35$

$$= -\underbrace{(3x^2 - 16x - 35)}$$

$$\begin{array}{r} 3 \cdot -35 = -105 \\ -3 \cdot 35 \\ 3 \cdot -35 \\ \hline 5 : 21 \end{array}$$

$$\begin{array}{r} -16x \\ = 5x - 21x \end{array}$$

x	-7
$3x$	$-21x$
5	-35

b) $4x^3 - 32x^2 + 64x$

$$= 4x(x^2 - 8x + 16)$$

$$= 4x(x-4)(x-4)$$

$\text{or } 4x(x-4)^2$

$$= -\underbrace{(3x+5)(x-7)}$$

or $(-3x-5)(x-7)$

c) $x^3 - 3x^2 - 4x + 12$

$$= (x^3 - 3x^2) - (4x - 12)$$

$$= \underbrace{x^2(x-3)}_{(x-3)} - \underbrace{4(x-3)}_{(x-3)}$$

$$= (x-3)(x^2 - 4)$$

$$= (x-3)(x+2)(x-2)$$